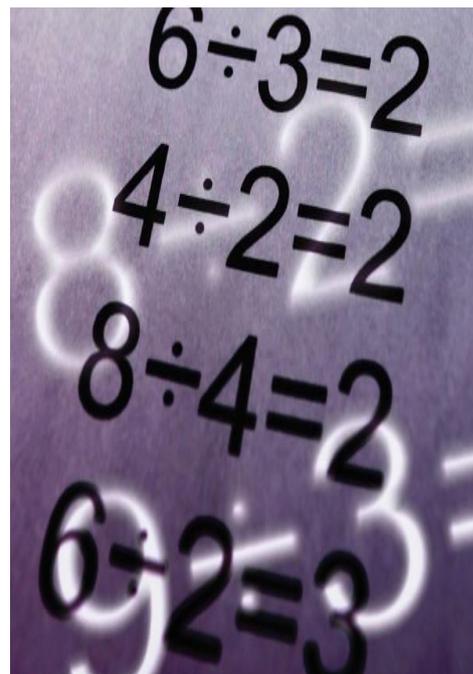


Pinner Park Junior School

Helping Your Child With Maths



CALCULATION

The maths work your child is doing at school may look very different to the kind of 'sums' you remember. This is because children are encouraged to work mentally, where possible, using personal jottings to help support their thinking. Even when children are taught more formal written methods (from late year 3 onwards), they are only encouraged to use these methods for calculations they cannot solve in their heads.

Discussing the efficiency and suitability of different strategies is an important part of maths lessons.

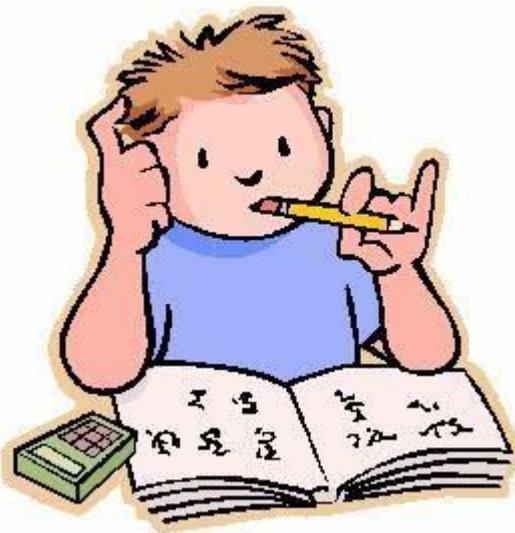
Talk to your child about how they work things out.

Ask your child to explain their thinking.



When faced with a calculation problem, encourage your child to ask.....

- ★ Can I do this in my head?
- ★ Could I do this in my head using drawings or jottings to help me?
- ★ Do I need to use a written method?



Also help your child to estimate and then check the answer. Encourage them to ask....

Is the answer sensible?

ADDITION

Children are taught to understand addition as combining two sets and counting on.

$$2 + 3 =$$

At a party, I eat 2 cakes and my friend eats 3 cakes. How many cakes did we eat altogether?



Children could draw a picture to help them work out the answer.

$$7 + 4 =$$

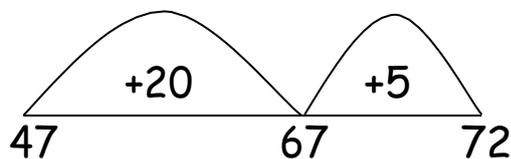
7 people are on the bus. 4 more get on at the next stop. How many people are on the bus now?



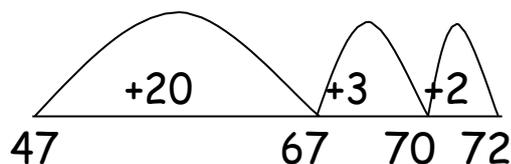
Children could use dots or tally marks to represent objects (quicker than drawing a picture).

$$47 + 25 =$$

My sunflower is 47cm tall. It grows another 25cm. How tall is it now?



or



Drawing an empty number line helps children to record the steps they have taken in a calculation (start on 47, +20, then +5). This is much more efficient than counting on in ones.

ADDITION (continued)

$$47 + 34 =$$

$$\begin{array}{r}
 \text{T U} \\
 47 \Rightarrow 40 + 7 \\
 + \underline{34} \Rightarrow \underline{30 + 4} \\
 \underline{81} \Leftarrow \underline{70 + 11}
 \end{array}$$

This method is known as partitioning. The children break down numbers into tens (T) and units (U), add each separately and then recombine to find the solution.

$$487 + 546 =$$

There are 487 boys and 546 girls in a school. How many children are there in school altogether?

$$\begin{array}{r}
 400 + 80 + 7 \\
 + 500 + 40 + 6 \\
 900 + 120 + 13 = 1033
 \end{array}$$

Moving to:

$$\begin{array}{r}
 546 \\
 + \underline{487} \\
 13 \\
 120 \\
 \underline{900} \\
 \underline{1033}
 \end{array}$$

Children will be taught written methods for those calculations they cannot do 'in their heads'. Expanded methods build on mental methods and make the value of the digits clear to children. The language used is very important:

(6 + 7, 40 + 80, 500 + 400, then 900 + 120 + 13 - *add this mentally NOT in columns*).

ADDITION (continued)

$$2.35 + 1.43 =$$

Two pounds thirty-five is added to one pound forty-three. How much is there altogether?

$$\begin{array}{r} 2 + 0.3 + 0.05 \\ + \underline{1 + 0.4 + 0.03} \\ \underline{3 + 0.7 + 0.08} = 3.78 \end{array}$$

Moving to:

$$\begin{array}{r} 2.35 \\ \underline{1.43} \\ 0.08 \\ 0.70 \\ \underline{3.00} \\ \underline{3.78} \end{array}$$

This method can then be used with decimals, using the context of money to begin.

$$12\ 786 + 2\ 568 =$$

12 786 people visited the museum last year. The numbers increased by 2 568 this year. How many people altogether visited this year?

$$\begin{array}{r} 1\ 2\ 7\ 8\ 6 \\ +\ 2\ 5\ 6\ 8 \\ \underline{1\ 5\ 3\ 5\ 4} \\ \quad \color{red}{1}\ \color{red}{1}\ \color{red}{1} \end{array}$$

When children are confident using the expanded method, this can be 'squashed' into the traditional compact method. Remember that the numbers are said according to their value. For example:

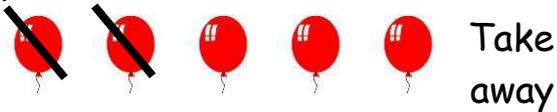
$$6 + 8, 80 + 60, 700 + 500, 2000 + 2000 \text{ (not } 2 + 2\text{)}.$$

SUBTRACTION

Children are taught to understand subtraction as taking away (counting back) and finding the difference (counting up or back).

$$5 - 2 =$$

I had five balloons. Two burst. How many did I have left?



Drawing a picture helps children to visualise the problem.

A teddy bear costs £5 and a doll costs £2. How much more does the bear cost?



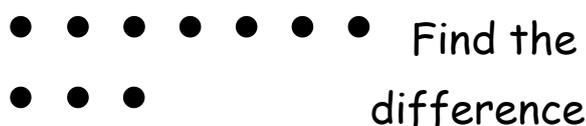
Children can compare quantities and count up or back to find the difference.

$$7 - 3 =$$

Mum baked 7 biscuits. I ate 3. How many were left?



Lisa has 7 felt tip pens and Tim has 3. How many more does Lisa have?

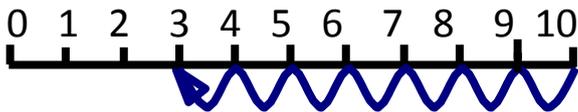


Using dots or tally marks is quicker than drawing a detailed picture.

SUBTRACTION (continued)

$$10 - 7 =$$

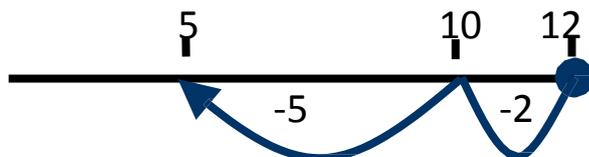
There were ten people on the bus. 7 people got off. How many people were left on the bus?



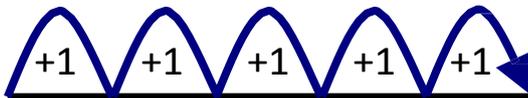
Children can count back in ones on a numbered line.

$$12 - 7 =$$

There were 12 children in a mixed class. 7 of the children were boys. How many girls were there in the class?



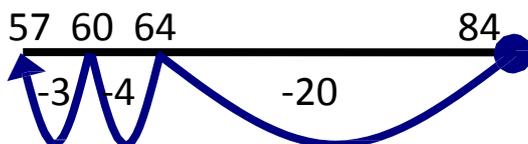
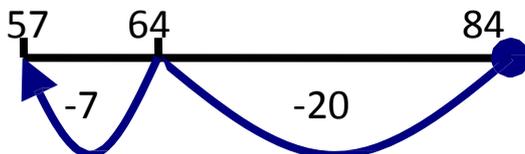
or



Using an empty number line to jump back in various amounts, choosing jumps of a sensible or manageable size.

$$84 - 27 =$$

I cut 27cm off a ribbon measuring 84cm. How much is left?

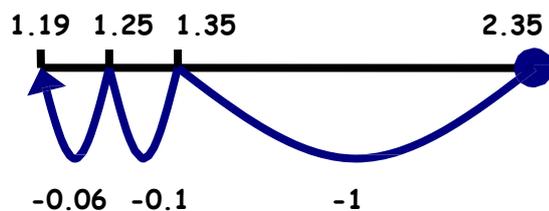


Children could count back using an empty number line. This is a really good way for them to record the steps they have taken (start on 84, -20, then -7).

SUBTRACTION (continued)

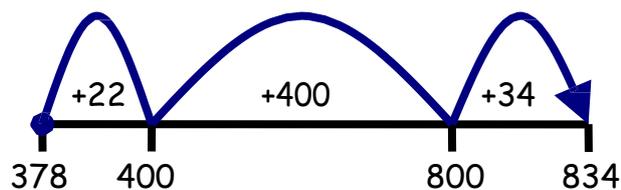
With decimals:

$$2.35 - 1.19$$



$$834 - 378 =$$

The library owns 834 books. 378 are out on loan. How many are on the shelves?



$$\begin{array}{r} 1.00 \\ 0.10 + \\ \hline 0.06 \\ \hline 1.16 \end{array}$$

Counting on / find the difference method:-

Children could count up (from smallest number to the biggest) using an empty number line. It is easiest to count up to a multiple of 10 or 100 (a friendly number).

$$74 - 27 =$$

$$\begin{array}{r} 70 + 4 \\ - \underline{20 + 7} \\ \hline 40 + 7 = 47 \end{array}$$

$$\begin{array}{r} 60 \\ \cancel{70} + 14 \end{array}$$

$$- \underline{20 + 7}$$

$$40 + 7 = 47$$

Expanded layout, leading to the Column Method.

Partitioning the numbers into tens and ones and writing one number under the other mirrors the column method, where ones are placed under ones and tens under tens.

SUBTRACTION (continued)

741 - 367 =

$$\begin{array}{r}
 700 + 40 + 1 \\
 - 300 + 60 + 7 \\
 \hline
 300 + 70 + 4
 \end{array}$$

$$\begin{array}{r}
 600 \quad 130 \quad 11 \\
 \cancel{700} + \cancel{40} + \cancel{1}
 \end{array}$$

$$\begin{array}{r}
 -300 + 60 + 7 \\
 \hline
 \end{array}$$

$$300 + 70 + 4$$

This does not link directly to mental methods of counting back or up but parallels the partitioning method for addition. It also relies on secure mental skills.

334 - 217 =

$$\begin{array}{r}
 3 \quad \cancel{3} \quad 4 \\
 - \quad \underline{2 \quad 1 \quad 7} \\
 1 \quad 1 \quad 7
 \end{array}$$

(Carrying tens to units)

537 - 274 =

$$\begin{array}{r}
 5 \quad \cancel{3} \quad 7 \\
 - \quad \underline{2 \quad 7 \quad 4} \\
 2 \quad 6 \quad 3
 \end{array}$$

(Carrying hundreds to tens)

The expanded method leads children to the more compact method or Column method sometimes known as Decomposition. The amount of time that should be spent teaching and practicing this method will depend on how secure the children are in their recall of number facts and with partitioning.

534 - 378 =

$$\begin{array}{r}
 5 \quad \cancel{3} \quad 4 \\
 - \quad \underline{3 \quad 7 \quad 8} \\
 1 \quad 5 \quad 6
 \end{array}$$

With decimals:

38.2 - 24.7 =

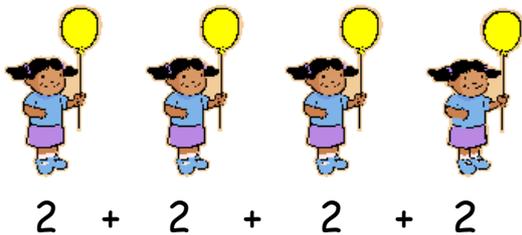
$$\begin{array}{r}
 3 \quad \cancel{8} \quad \cdot 2 \\
 - \quad \underline{2 \quad 4 \quad \cdot 7} \\
 1 \quad 3 \quad \cdot 5
 \end{array}$$

MULTIPLICATION

Children are taught to understand multiplication as repeated addition and scaling. It can also describe an array.

$$2 \times 4 =$$

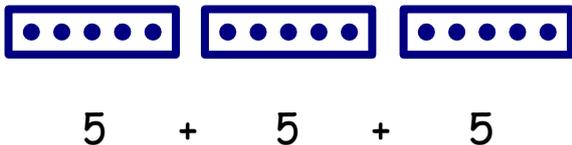
Each child has two eyes. How many eyes do four children have?



Again a picture can be useful.

$$5 \times 3 =$$

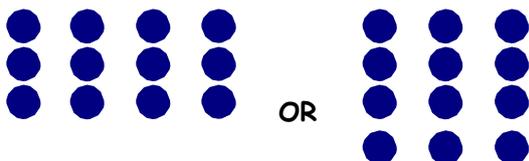
There are 5 cakes in a pack. How many cakes in 3 packs?



Dots or tally marks are often drawn in groups. This shows 3 groups of 5 or 3 lots of 5.

$$4 \times 3 =$$

A chew costs 4p. How much do 3 chews cost.

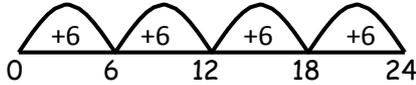


Drawing an array (3 rows of 4 or 3 columns of 4) gives children an image of the answer. It also helps develop the understanding that 4×3 (4 three times) is the same as 3×4 (3 four times).

MULTIPLICATION (continued)

6x4=

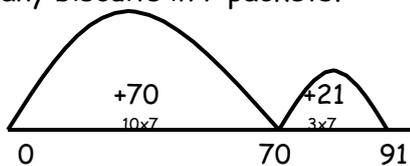
There are 4 cats. Each cat has 6 kittens. How many kittens are there altogether?



Children could count on in equal steps, recording each jump on an empty number line. This shows 4 jumps of 6.

13x7=

There are 13 biscuits in a packet. How many biscuits in 7 packets?



When numbers get bigger, it is inefficient to do lots of small jumps. Split 13 into parts (10 and 3). This gives you two jumps (10x7 and 3x7).

6x124=

124 books were sold. Each book cost £6. How much money was taken?

$$\begin{array}{r|l} & 100 \quad 20 \quad 4 \\ \hline 6 & 600 \quad 120 \quad 24 \quad = 744 \end{array}$$

This is called the grid method. 124 is partitioned (100, 20 and 4) and each of these is multiplied by 6. The three answers are then added together.

72x34=

A cat is 72cm long. A tiger is 34 times longer. How long is the tiger?

$$\begin{array}{r|l} & 70 & 2 \\ \hline 30 & 2100 & 60 & = 2160 \\ 4 & 280 & 8 & = \underline{288} \\ & & & 2448 \end{array}$$

This method also works for larger numbers.

Again split up the numbers and multiply each part. Add across the rows, then, add those two answers together.

MULTIPLICATION (Expanded Method)

Expanded method

$$\begin{array}{r}
 30+8 \\
 \times \quad 7 \\
 \hline
 56 \quad (7 \times 8) \\
 \underline{210} \quad (7 \times 30) \\
 266
 \end{array}$$

Leading to

$$\begin{array}{r}
 38 \\
 \times \quad 7 \\
 \hline
 56 \quad (7 \times 8) \\
 \underline{210} \quad (7 \times 30) \\
 266
 \end{array}$$

The next step is to represent the method of recording in a column format, but showing the working. Draw attention to the links with the grid method above.

Children should describe what they do by referring to the actual values of the digits in the columns. For example, the first step in 38×7 is 'thirty multiplied by seven', not 'three times seven', although the relationship between 3×7 should be stressed

Long Multiplication

$$\begin{array}{r}
 38 \\
 \times 7 \\
 \hline
 \underline{266} \\
 5
 \end{array}$$

124×26

$$\begin{array}{r}
 124 \\
 \times 26 \\
 \hline
 7'4'4 \\
 \underline{2480} \\
 3224
 \end{array}$$

The recording is reduced further, with carry digit recorded below the line or above the top number.

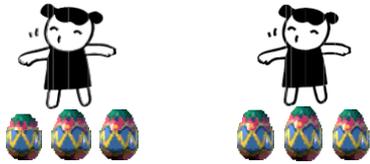
If, after practice, children cannot use the compact method without making errors, they should return to the expanded format.

DIVISION

Children are taught to understand division as sharing and grouping.

$$6 \div 2 =$$

6 eggs are shared between 2 children. How many eggs do they get each?



Sharing
between two

There are 6 eggs. How many children can have two each?



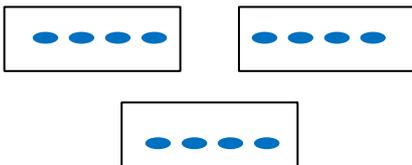
Grouping in
twos

More pictures!

Drawing often gives children a way into solving the problem.

$$12 \div 4 =$$

4 apples are packed in a basket. How many baskets can you fill with 12 apples?

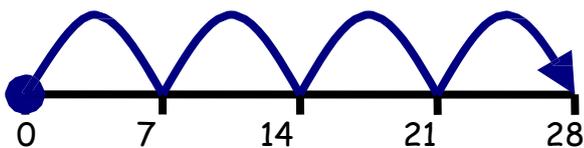


Grouping
in fours

Dots or tally marks can either be shared out one at a time or split up into groups.

$$28 \div 7 =$$

A chew bar costs 7p. How many can I buy with 28p.

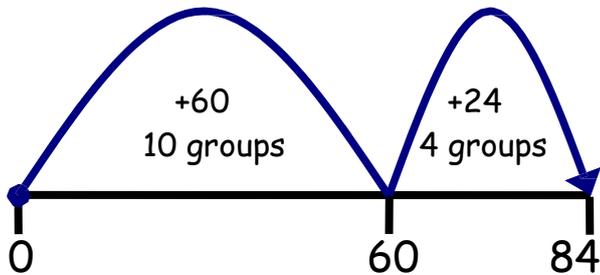


To work out how many 7s there are in 28, draw jumps of 7 along a number line. This shows you need 4 jumps of 7 to reach 28.

DIVISION (continued)

$84 \div 6 =$

I need 6 drawing pins to put up a picture. How many pictures can I put up with 84 pins?



It would take a long time to jump in sixes to 84 so children can jump on in bigger 'chunks'. A jump of 10 groups of 6 takes you to 60. Then you need another 4 groups of 6 to reach 84. Altogether, that is 14 sixes.

$184 \div 7 =$

I need 184 chairs for a concert. I arrange them in rows of 7. How many rows do I need?

$$\begin{array}{r}
 026 \text{ r. } 2 \\
 7 \overline{) 184} \\
 \underline{- 140} \quad \text{20 groups} \\
 44 \\
 \underline{- 42} \quad \text{6 groups} \\
 2
 \end{array}$$

$= 26 \text{ r}2$

This method is known as chunking. In this example, you are taking away chunks of 7. First subtract 140 (20 groups of 7) and you are left with 44. Then subtract 42 (6 groups of 7), to leave 2. Altogether, that is 26 sevens with a remainder of 2.

DIVISION (continued)

Long Division

$432 \div 15$ becomes

$$\begin{array}{r} 28 \text{ r } 12 \\ 15 \overline{) 432} \\ \underline{300} \\ 132 \\ \underline{120} \\ 12 \end{array}$$

$432 \div 15$ becomes

$$\begin{array}{r} 28 \\ 15 \overline{) 432} \\ \underline{300} \\ 132 \\ \underline{120} \\ 12 \end{array} \begin{array}{l} 15 \times 20 \\ 15 \times 8 \end{array}$$

$432 \div 15$ becomes

$$\begin{array}{r} 28.8 \\ 15 \overline{) 432.0} \\ \underline{300} \quad \downarrow \\ 132 \quad \downarrow \\ \underline{120} \quad \downarrow \\ 120 \\ \underline{120} \\ 0 \end{array}$$

$$\frac{12}{15} = \frac{4}{5}$$

Answer: $28 \frac{4}{5}$

Answer: 28.8

The long division method leads on from the chunking method.

Answers can be given as a fraction, decimal or with a remainder.

This method is useful when dividing with larger numbers.

Short Division

$98 \div 7$ becomes

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \\ \underline{70} \\ 28 \\ \underline{28} \\ 0 \end{array}$$

Answer: 14

$432 \div 5$ becomes

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \\ \underline{400} \\ 32 \\ \underline{30} \\ 2 \end{array}$$

Answer: 86 remainder 2

$496 \div 11$ becomes

$$\begin{array}{r} 45 \text{ r } 1 \\ 11 \overline{) 496} \\ \underline{440} \\ 56 \\ \underline{55} \\ 1 \end{array}$$

Answer: $45 \frac{1}{11}$

The short division method is a more compact method which is most useful when dividing by smaller numbers.

Counting Ideas

● Practise chanting the number names. Encourage your child to join in with you. When they are confident, try starting from different numbers - 4, 5, 6 ...



● Sing number rhymes together – there are lots of commercial apps and CDs available



● Give your child the opportunity to count a range of interesting objects (coins, pasta shapes, buttons etc.). Encourage them to touch and move each object as they count.



● Count things you cannot touch or see (more difficult!!). Try lights on the ceiling, window panes, jumps, claps or oranges in a bag.



● Play games that involve counting (e.g. snakes and ladders, dice games, games that involve collecting objects).



● Look for numerals in the environment. You can spot numerals at home, in the street or when out shopping.



● Cut out numerals from newspapers, magazines or birthday cards. Then help your child to put the numbers in order.



● Make mistakes when chanting, counting or ordering numbers. Can your child spot what you have done wrong?



● Choose a number of the week e.g. 5. Practise counting to 5 and on from 5. Count out groups of 5 objects (5 dolls, 5 bricks, 5 pens). See how many places you can spot the numeral 5.

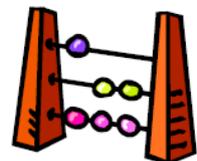


Real Life Problems

- ❖ Go shopping with your child to buy two or three items. Ask them to work out the total amount spent and how much change you will get.
- ❖ Buy some items with a percentage extra free. Help your child to calculate how much of the product is free.
- ❖ Plan an outing during the holidays. Ask your child to think about what time you will need to set off and how much money you will need to take.
- ❖ Use a TV guide. Ask your child to work out the length of their favourite programmes. Can they calculate how long they spend watching TV each day / week?
- ❖ Use a bus or train timetable. Ask your child to work out how long a journey between two places should take? Go on the journey. Do you arrive earlier or later than expected? How much earlier or later?
- ❖ Help your child to scale a recipe up or down to feed the right amount of people.
- ❖ Work together to plan a party meal on a budget.



These are just a few ideas to give you a starting point. Try to involve your child in as many problem-solving activities as possible. The more 'real' a problem is, the more motivated they will be when trying to solve it.



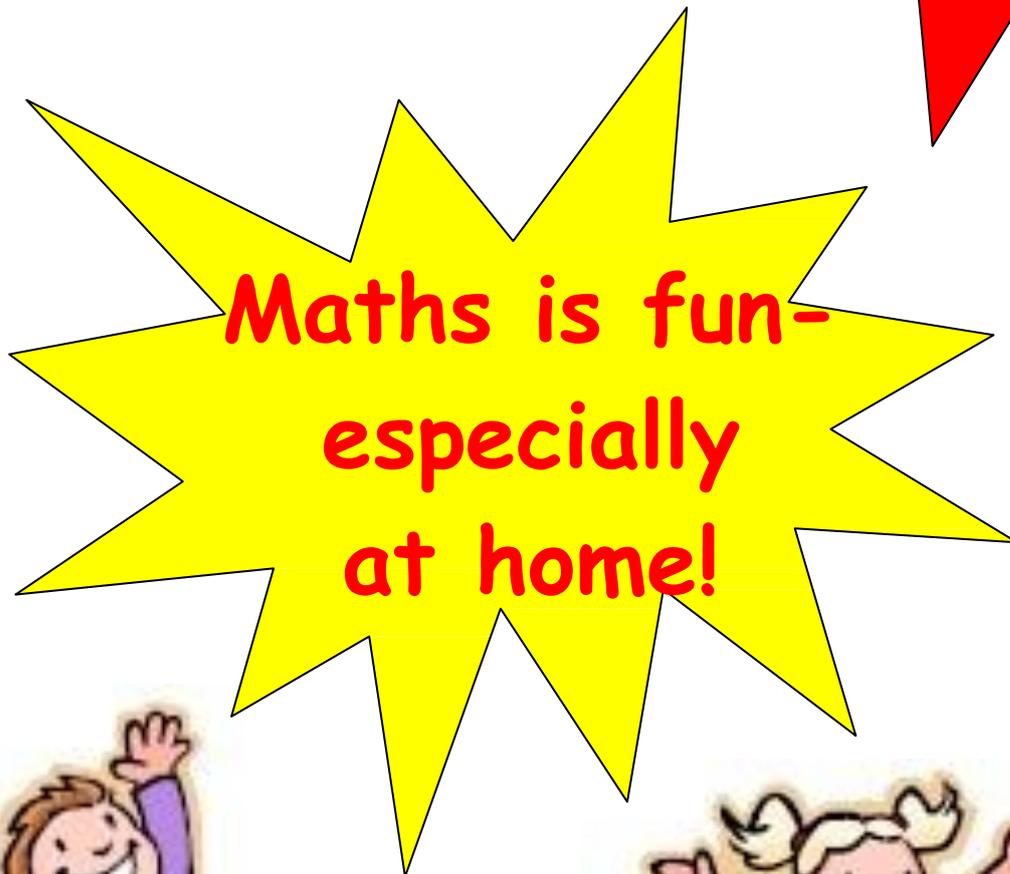
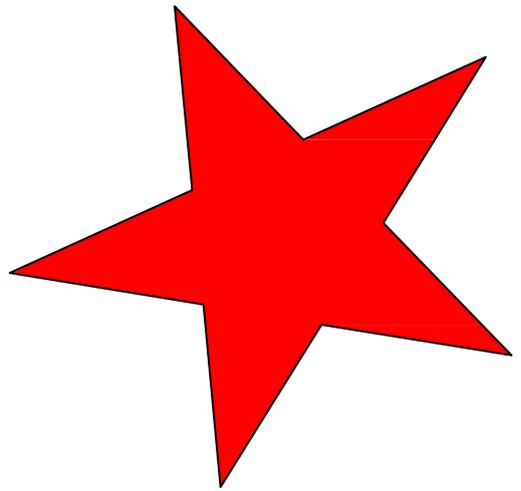
PRACTISING NUMBER FACTS

- ✚ Find out which number facts your child is learning at school (addition facts to 10, times tables, doubles etc). Try to practice for a few minutes each day using a range of vocabulary.
- ✚ Have a 'fact of the day'. Pin this fact up around the house. Practise reading it in a quiet, loud, squeaky voice. Ask your child over the day if they recall the fact.
- ✚ Play 'ping pong' to practice complements with your child. You say a number. They reply with how much more is needed to make 10. You can also play this game with numbers totaling 20, 100 or 1000. Encourage your child to answer quickly, without counting or using fingers.
- ✚ Throw 2 dice. Ask your child to find the total of the numbers (+), the difference between them (-) or the product (x). Can they do this without counting?
- ✚ Use a set of playing cards (no pictures). Turn over two cards and ask your child to add or multiply the numbers. If they answer correctly, they keep the cards. How many cards can they collect in 2 minutes?
- ✚ Play Bingo. Each player chooses five answers (e.g. numbers to 10 to practice the five times tables). Ask a question and if a player has the answer, they can cross it off. The winner is the first one to cross off all their answers.
- ✚ Give your child an answer. Ask them to write as many addition sentences as they can with this answer. (e.g. $10 = \square + \square$). Try with multiplication or subtraction.
- ✚ Give your child a number fact (e.g. $5 + 3 = 8$). Ask them what else they can find out from this fact (e.g. $3 + 5 = 8$, $8 - 5 = 3$, $8 - 3 = 5$, $50 + 30 = 80$, $500 + 300 = 800$, $5 + 4 = 9$, $15 + 3 = 18$). Add to the list over the next few days. Try starting with a 'x' fact as well.

Shapes and Measures



- ❖ Choose a shape of the week e.g. cylinder. Look for this shape in the environment (tins, candles etc). Ask your child to describe the shape to you (2 circular faces, 2 curved edges...).
- ❖ Play 'guess my shape'. You think of a shape. Your child asks questions to try to identify it but you can only answer 'yes' or 'no' (e.g. Does it have more than 4 corners? Does it have any curved sides?)
- ❖ Hunt for right angles around your home. Can your child also spot angles bigger or smaller than a right angle?
- ❖ Look for symmetrical objects. Help your child to draw or paint symmetrical pictures / patterns.
- ❖ Make a model using boxes / containers of a different shapes and sizes. Ask your child to describe their model.
- ❖ Practise measuring the lengths or heights of objects (in metres or cm). Help your child to use different rulers and tape measures correctly. Encourage them to estimate before measuring.
- ❖ Let your child help with cooking at home. Help them to measure ingredients accurately using weighing scales or measuring jugs. Talk about what each division on the scale stands for.
- ❖ Choose some food items out of the cupboard. Try to put the objects in order of weight, by feel alone. Check by looking at the amounts on the packets.
- ❖ Practise telling the time with your child. Use both digital and analogue clocks. Ask your child to be 'timekeeper' (e.g. tell me when it is half past four because then we are going swimming).
- ❖ Use a stop clock to time how long it takes to do everyday tasks (e.g. how long does it take to get dressed?). Encourage your child to estimate first.



**Give your child lots of
praise and encouragement**